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Test for Diregence: if an does not so, it direges

Geometric? & air , som is ai coverages for

1-1-1

F-sorres?  $\frac{1}{N}$  converges for p>1, other se denominations of  $\sum_{i=1}^{n} f(x_i)$  is convergent,  $\sum_{i=1}^{n} a_{n_i}$  is convergent if  $\sum_{i=1}^{n} f(x_i)$  is direct,  $\sum_{i=1}^{n} a_{n_i}$  is direct

estable  $R_n = s - s_n$ ,  $\int_{n+1}^{\infty} f(s) ds \leq R_n \leq \int_{n}^{\infty} f(s) ds$  $R_n \leq accuracy$   $s_n + S_{n+1} \cdot f(s) ds \leq s \leq S_n^{\infty} f(s) ds^{+} s_n$ 

Comparison: Earn and Elen are both 20 for elln

If the life on diverges, on conveyes

If he conveyes, an conveyes

If I'm on = c and c>0, then both corresponds or whole dange

Alternalmy socies

differentiag if an ani <0let 5n = land if bn+1 bn = 0 if converges (use test for all an allow bn = 0 if converges (use test for all and bn = 0 bn = 0).

bar & accord

Power Series \_ C. (x-a)

Three possibilities, i) series converges only when x=a

11) series conveges for all x

iii) series conveners if Ix-a/ < R

duringes if Ix-al > R

R= 1/2 , if L=0, Risall values of x test bandaris

Taylor and Maclaurih series

Madavin series where a=0

$$(1+x)^{K} = \sum_{n=0}^{\infty} {K \choose n} x^{n}, \text{ where } (K) = \frac{K(k-1)\cdots(k-n+1)}{n!}$$
for  $n \ge 1$ , and  $(K) = 1$ 

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# Madaurin Series

$$e^{x} = \sum_{n=0}^{\infty} \frac{x^{n}}{n!}$$

$$\sin x = \sum_{n=0}^{\infty} (-1)^{n} \frac{x^{2n+1}}{(2n+1)!}$$

$$\cos x = \sum_{n=0}^{\infty} (-1)^{n} \frac{x^{2n}}{(2n)!}$$

$$\tan x^{2n} = \sum_{n=0}^{\infty} (-1)^{n} \frac{x^{2n}}{(2n+1)!}$$

$$\int_{1-x}^{1} = \sum_{n=0}^{\infty} x^{n}$$

$$\int_{1-x}^{1} \cos x^{n} = \int_{1-x}^{1} (-1, 1)$$

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Separable equation

$$\frac{dy}{dx} = h(y)g(x) \implies \int \frac{dy}{h(y)} = \int g(x)dx$$

$$note! \ y(x) = G(x) + C$$

Honogreous Equation

$$\frac{dx}{dx} = f(x,y) \text{ where } f(x,y) \text{ can be written as } g(\frac{x}{x})$$
where  $f(x,y)$  can be written as  $g(\frac{x}{x})$ 
where  $f(x,y)$  can be written as  $g(\frac{x}{x})$ 

First Order linear Equation

$$\frac{dy}{dx} + P(x)y = Q(x) \qquad \mu = e^{\int P(x) dx}$$

$$Y = \frac{1}{N} \left( \int \rho Q(x) dx + C \right)$$

First Order Exact Equation

$$P(x,y) + Q(x,y) \frac{dx}{dx} = 0 \quad \text{is exact if} \quad \frac{\partial P}{\partial y} = \frac{\partial Q}{\partial x}$$

- O then, integrate Por a in terms of x or y (gives constant t)
- 10 then, differentiate SPdx or SQdy in terms of y or x
- 10 this will give g'(y) or g'(x) which is = to Q or P
- 9 giving what g'(y) or g'(x) is
- O then integrate for for equation O

Note: if not exact, use integraling factor

$$(I)\left(\frac{P_{x}-Q_{x}}{Q}\right)=\frac{dI}{dx}$$
, solve for I

multiply equation by I. It is now exect (do a test too)

# Second Order Linear Equation

$$P(x) \frac{d^2y}{dx^2} + Q(x) \frac{dy}{dx} + R(x)y = G(x)$$

if G(x)=0, then hangyerpass, if G(x) ≠0, then non-honogeneous

### if honogeneous / constant conflictiont

then art for + c = 0 , solve for r

if decriment, D = b2-4ac >0, then

if D=0, then r,= r2, :

if DKO, then ri= a+i/s, r2= x-i/s

$$y_i(x) = e^{r_i x}$$
 $y_i = e^{r_i x}$ 
 $y_i = e^{r_i x}$ 

rote: 
$$e^{-ix} = co\theta + ixn\theta$$
,  $y_{i} = e^{ix} (cospx - ixnpx)$   
so  $y = e^{ix} (c_{i}cospx + c_{i}sinpx)$ 

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Non-Honogeneous Linear Equations

if constant coefficients, ay'' + by' + cy = G(x)complemently equivary the sy' + cy = 0 y6)=40+40

let  $y=e^{x}$ ,  $ar^{2}+br+c=0$ , find r solve for y like is done for the homogeneous way

then make up yo

 $\begin{cases}
if G(x) = C_{n}x^{n} + ... + C_{1}x + C_{0} \\
try y(p) = A_{n}x^{n} + ... + A_{1}x + A_{0}
\end{cases}$   $\begin{cases}
if G(x) = C_{e}^{kx} \\
try y(p) = A_{e}^{kx}
\end{cases}$   $\begin{cases}
if G(x) = C_{e}^{kx} + D_{e}^{kx}
\end{cases}$ 

if any term of yp is in ye, multiply yp by x (or x²,ele)

put ye", ye', ye into equation, solve for constants

Vacintion of parametes (2nd order, non-honogeneon, constant coefficient)

find ye = c, y, + cz yz from ay" + by '+ cy =0

then  $u_1'y_1 + u_2'y_2 = 0$  $u_1'y_1' + u_2'y_2' = GG)$ 

1 try ylp) = Acoskx + Bankx

some for u, , uz then you u, y, + uzyz u; = [0]

y = ye + yo

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#### series solutions 2nd order / non-constant coefficient

cassume  $y = \sum_{n=0}^{\infty} c_n x^n$ , find y', y'', put indees to the same put into equ, put together then the constant start = 0 write out constants for n=0,1,2,3, etc. find a pattern (in terms of first far  $c_n s$ )

Put back into equ.  $y = c_0 + c_1 x + c_2 x^2 + \dots$ suplify - is it maximum? Yes-simplify